

AMENDMENTS TO THE CLAIMS:

This listing of claims will replace all prior versions, and listings, of claims in the application:

LISTING OF CLAIMS:

1. (Currently Amended) A cryptographic system ~~combining the so-called discrete logarithm and factorization principles,~~ comprising at least one of an encryption system and a decryption system that utilizes, among other things, public keys and a secret key, wherein the said public keys comprise, at least:

a. an RSA modulus n , greater in size than 640 bits, having the following property:

$$n = (A p_A + 1) \times (B p_B + 1)$$

in which:

p_A and p_B are prime numbers greater in size than 320 bits,

$(A p_A + 1)$ is an RSA prime denoted p ,

$(B p_B + 1)$ is an RSA prime denoted q ,

A is the product of $k/2$ (k being an even integer number between 10 and 120) prime numbers (denoted $p[i]$, $i = 1$ to $k/2$) of relatively small size (between 2 and 16 bits) and

B is the product of $k/2$ prime numbers (also denoted $p[i]$, $i = k/2 + 1$ to k);

the $p[i]$ s being of relatively small size (between 2 and 16 bits), and also able to be mutually prime;

b. an exponentiation base g , of order $\Phi(n)/4$ (where $\Phi(n)$ denotes the Euler indicator function), g therefore having not to be a $p[i]$ -th power modulo n of any number.

2. (Currently Amended) A cryptographic system according to Claim 1 comprising at least an encryption/decryption system[[1]], wherein the encryption of a message m , $m < AB$, ~~consists of~~ comprises the operation:

$$c = g^m \bmod n$$

where c denotes the cryptograph (encrypted message).

3. (Currently Amended) A cryptographic system according to Claim 2 comprising an encryption/decryption system, wherein the integrity of a message m can be provided by the encryption of $m|h(m)$ (h denoting a hashing function and $|$ denoting concatenation), or by the encryption of DES (key, m), ~~the~~ where said key ~~being~~ is a key accessible to all.

4. (Currently Amended) A cryptographic system according to Claim 1 comprising an encryption/decryption system, and a key escrow system, wherein the ~~said~~ secret key of the a decrypter or of the an escrow ~~centre~~ authority is the number $\Phi(n)$, and ~~in that~~ wherein the operation of decryption or of recovering the identity of a user ~~consists of~~ comprises the following steps:

a. calculating, for i from 1 to k : $y[i] = c^{\Phi(n)/p[i]} \bmod n$;

b. for i from 1 to k

for j from 1 to $p[i]$

comparing $y[i]$ with the values $g^{j\Phi(n)/p[i]} \bmod n$ independent of m ;

if $g^{j\Phi(n)/p[i]} \bmod n = y[i]$ then assign $\mu[i] = j$

c. reconstructing ~~the~~ a message m from the Chinese remainder theorem CRT and the values $\mu[i]$.

5. (Currently Amended) A cryptographic system according to Claim 4 ~~or 5~~ comprising an encryption/decryption system and a key escrow system, ~~the~~ wherein said decrypter speeds up the calculation of the quantities $y[i]$ by calculating:

a) $z = c^r \bmod n$ where $r = p \wedge p_B$

b) for i from 1 to k : $y[i] = z^{AB/p[i]} \bmod n$,

so as to take advantage of the difference in size between $AB/p[i]$ and $\Phi(n)/p[i]$ for speeding up the calculations.

6. (Currently Amended) A cryptographic system according to Claim 4 comprising an encryption/decryption system and a key escrow system ~~or 5~~, wherein the decrypter pre-calculates and saves, once and for all, the table of values $g^{j\Phi(n)/p[i]} \bmod n$ for $1 \leq i \leq k$ and $1 \leq j \leq p[i]$

or,

~~more specifically~~, a truncation or a hashing of these values (denoted h) having the following property:

$$h(g^{j\Phi(n)/p[i]} \bmod n) \neq h(g^{j'\Phi(n)/p[i]} \bmod n) \text{ if } j \neq j'.$$

7. (Currently Amended) A cryptographic system according to any one of ~~Claim~~ Claims 4 to 6 comprising an encryption/decryption system and a key escrow system, wherein the decrypter speeds up its calculations by separately decrypting the message modulo p and then modulo q , and constructing the modulo results with the help of the Chinese remainder theorem in order to find m again.

8. (Currently Amended) A cryptographic system according to ~~any one of Claims 4 to 7~~ Claim 4, wherein a key escrow ~~centre or authority implemented~~ implements the following steps:

a. it codes the identify of the user $ID = \sum 2^{i-1} ID[i]$ where $ID[i]$ are the bits of the identity of the said user of the system (the sum being taken for I from 1 to k) by calculating $e(ID) = \prod p[i]^{ID[i]}$ (the product being taken for I from 1 to k);

b. it issues, to the user, an El-Gamal key (that is to say an exponentiation base) $c = g^{e(ID)u} \bmod n$,

in which u is a large random prime or a number prime with $\Phi(n)$;

c. it thus makes it possible for the user to derive, from c , his El-Gamal public key by choosing a random number x and raising c to the power x ~~modulo n~~ modulo n ;

d. with the aim of finding the trace of the user, the authority extracts, from ~~the~~ an El-Gamal cryptogram of ~~the~~ an encrypter, ~~the~~ said cryptogram always comprising two parts, the part:

$$v = c^r \bmod n$$

where r is the encryption random number chosen by the ~~encrypter~~ encrypter;

e. knowing $\Phi(n)$, ~~the~~ said authority finds the bits $ID[i]$ by means of the following algorithm:

1. calculate, for i from 1 to k : $y[i] = v^{\Phi(n)/p[i]} \bmod n$

2. if $y[i] = 1$, then $\mu[i] = 1$, otherwise $\mu[i] = 0$

3. calculate:

$$ID' = \sum 2^{i-1} \mu[i]$$

4. find: $ID = CCE(ID')$

in which CCE denotes an error correction mechanism.

9. (Currently Amended) A cryptographic system according to ~~any one of Claims 4 to 7~~ Claim 4 comprising a key escrow system, ~~it is based on the so-called a~~ Diffie-Hellman key exchange mechanism where a number c , obtained by raising g to a random power a modulo n by one ~~of the parties~~ party, is intercepted by ~~the~~ said escrow authority:

$$c = g^a \bmod n$$

~~the~~ said escrow authority finds a again in the following manner:

a. knowing the factorization of n , ~~the~~ said authority finds, with the help of the decryption algorithm, the value

$$\alpha = a \bmod AB$$

that is $a = \alpha + \beta AB$;

b. ~~the~~ said authority calculates: $\lambda = c/g^\alpha \bmod n = g^{\beta AB} \bmod n$

c. using a cryptanalysis algorithm, the authority calculates the discrete logarithm β

$$\lambda = (g^{AB})^\beta \bmod n$$

d. the authority finds

$$a = \alpha + \beta AB$$

and decrypts the communications based on the use of a .

10. A cryptographic system according to ~~any one of Claims 2 to 9~~ Claim 2 comprising an encryption/decryption system and a key escrow system, wherein the RSA modulus n is the product of three factors:

$$n = (A p_A + 1) \times (B p_B + 1) \times (C p_C + 1)$$

in which p_A , p_B , p_C are prime numbers greater in size than 320 bits,

$(A p_A + 1)$, $(B p_B + 1)$, $(C p_C + 1)$ are RSA primes, denoted respectively p , q , r ,

A , B and C are each the product of $k/3$ prime numbers (denoted $p[i]$, $i = 1$ to k), the $p[i]$ s being of relatively small size (between 2 and 16 bits) and able to be mutually prime numbers and k being an integer number between 10 and 120, so that the product ABC has at least 160 bits.

Claims 11-12. (Canceled)

13. (Currently Amended) A cryptographic system ~~wherein~~ including at least one of an encryption system and a decryption system that uses a public key and a private key ~~are used~~ in providing secure encryption and decryption of a message m , the public key comprising:

an RSA modulus n , wherein n is greater than 640 bits, and wherein $n = (A p_A + 1)(B p_B + 1)$, wherein p_A and p_B are prime numbers greater in size than 320 bits, $(A p_A + 1)$ is an RSA prime denoted p , $(B p_B + 1)$ is an RSA prime denoted q , A is the product of $k/2$ prime numbers $p[i]$, $i = 1$ to $k/2$, B is the product of $k/2$ prime numbers $p[i]$, $i = 1$ to $k/2$, the $p[i]$'s being mutually prime, and wherein k is an even integer; and

an exponentiation base g , wherein g is of the order $\Phi(n)/4$, $\Phi(n)$ being the Euler indicator function.

14. (Previously Presented) The cryptographic system of claim 13, wherein the message m is encrypted into a cryptogram c according to $c = g^m \bmod n$.

15. (Currently Amended) The cryptographic system of claim 14, wherein the integrity of the message m can be provided by the encryption $m|h(m)$ wherein $h(m)$ is a hashing function and $|$ ~~denoting~~ denotes concatenation.

16. (Previously Presented) The cryptographic system of claim 14, wherein the integrity of the message m can be provided by the encryption of a DES key, wherein the DES key is publicly available.

17. (Previously Presented) The cryptographic system of claim 13, wherein the secret key is equal to $\Phi(n)$, and wherein decryption of the message m according to reconstructing the message m from the Chinese remainder theorem CRT and the values $\mu[i]$, where $\mu[i] = j$ when $g^{j\Phi(n)/p[i]} \bmod n = y[i]$, $y[i] = c^{\Phi(n)/p[i]} \bmod n$.

18. (Currently Amended) The cryptographic system of claim 17, wherein the decrypter speeds up its calculations by separately decrypting the ~~messgae~~ message modulo p and then modulo q , and constructing the modulo results with the help of the Chinese remainder theorem to obtain the message m .

19. (Previously Presented) The cryptographic system of claim 17, further comprising:

an El-Gamal key $c = g^{e(ID)u} \bmod n$, wherein u is a large random prime, $ID = \sum_{i=1}^{l-1} ID[i]$, $ID[i]$ representing bits of the identity of a user of the system.

20. (Previously Presented) A method of encrypting a message m , comprising:

calculating n according to $n = (Ap_A + 1)(Bp_B + 1)$, wherein p_A and p_B are prime numbers greater in size than 320 bits, $(Ap_A + 1)$ is an RSA prime denoted p , $(Bp_B + 1)$ is an RSA prime denoted q , A is the product of $k/2$ prime numbers $p[i]$, $i = 1$ to $k/2$, B is the product of $k/2$ prime numbers $p[i]$, $i = 1$ to $k/2$, the $p[i]$'s being mutually prime, and wherein k is an even integer; and

calculating a cryptogram of the message m according to $c = g^m \bmod n$, wherein the exponentiation base g is of the order $\Phi(n)/4$, $\Phi(n)$ being the Euler indicator function.

21. (Previously Presented) The method of claim 20, wherein the message m is decrypted, further comprising:

calculating for $i = 1$ to k : $y[i] = c^{\Phi(n)/p[i]} \bmod n$;

comparing $y[i]$ with values $g^{j\Phi(n)/p[i]} \bmod n$ independent of m , for I from 1 to k and j from 1 to $p[i]$;

if $g^{j\Phi(n)/p[i]} \bmod n = y[i]$ then assign $\mu[i] = j$; and

reconstructing the message m from the Chinese remainder theorem CRT and the values $\mu[i]$.

22. (Previously Presented) The method of claim 21, wherein the decrypter speeds up the calculation of the quantities $y[i] = z^{A/p[i]}$ by calculating $z = c^r \bmod n$ where $r = p_A p_B$ for $= 1$ to k .

23. (Previously Presented) The method of claim 21, wherein the decrypter calculates and saves the table of values $g^{j\Phi(n)/p[i]} \bmod n$ for i from 1 to k and j for 1 to $p[i]$.